Grayscale Opening and Closing

- The expression for grayscale opening and closing is the same as for binary
- The expression for opening is

$$f \circ b = (f \ominus b) \oplus b$$

which is simply erosion followed by dilation

- The expression for closing is

$$f \bullet b = (f \oplus b) \ominus b$$

which is simply dilation followed by erosion

Geometric Interpretation

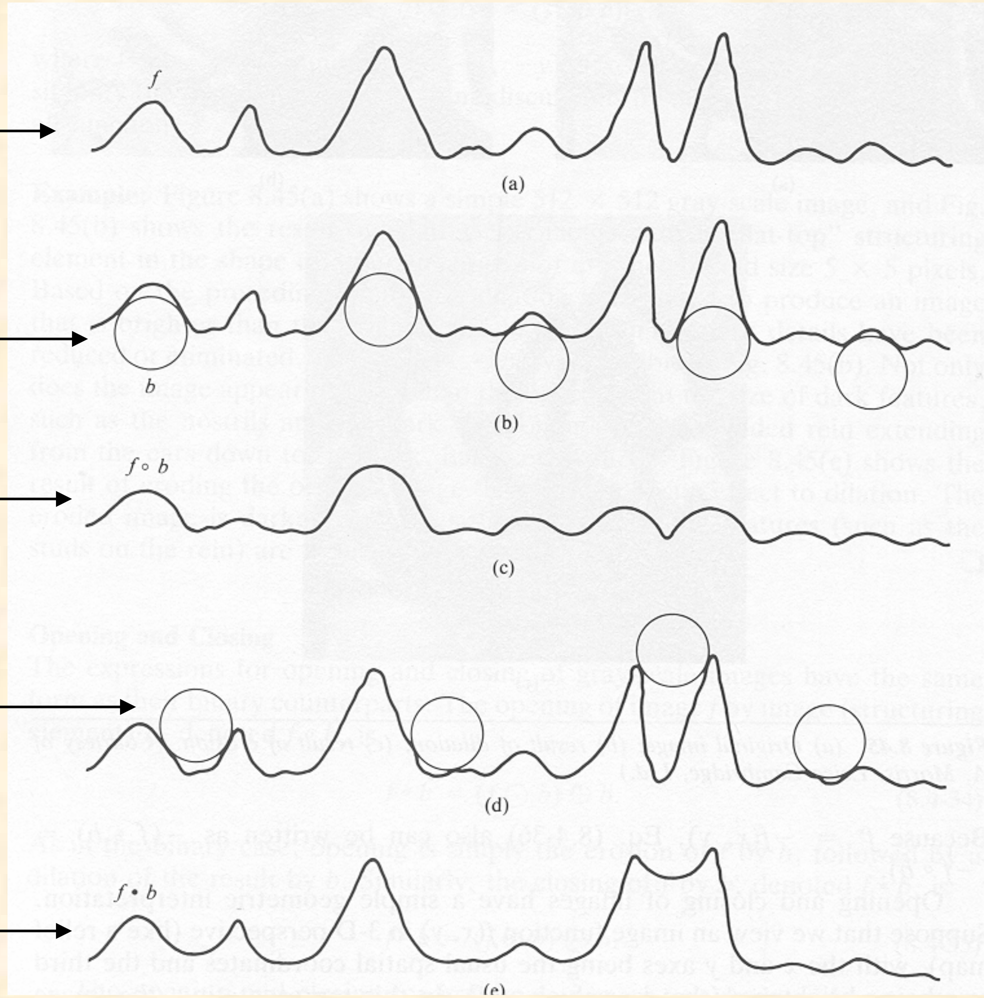
scanline →

rolling ball below →

opening →

rolling ball above →

closing →



Rolling Ball Interpretation

Comments

- Openings are used to remove small light details, while leaving the overall gray levels and larger bright features relatively undisturbed
- Closing is generally used to remove dark details from an image while leaving bright features relatively undisturbed

Applications

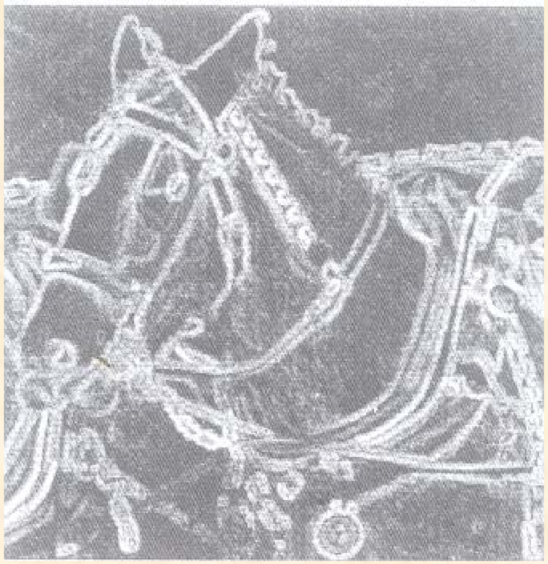
- Morphological smoothing
  - Opening followed by a closing
  - removes or attenuates both bright and dark artifacts or noise
- Morphological gradient
  - This is the difference between dilation and erosion

$$g = (f \oplus b) - (f \ominus b)$$

  - highlights sharp gray level transitions in the image
  - depends less on edge direction than Sobel etc

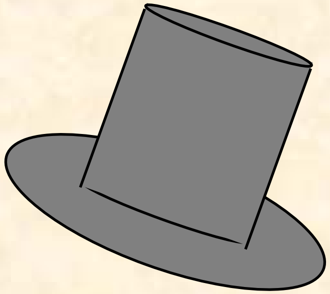
Examples

Morphological Smoothing



Morphological Gradient

Applications



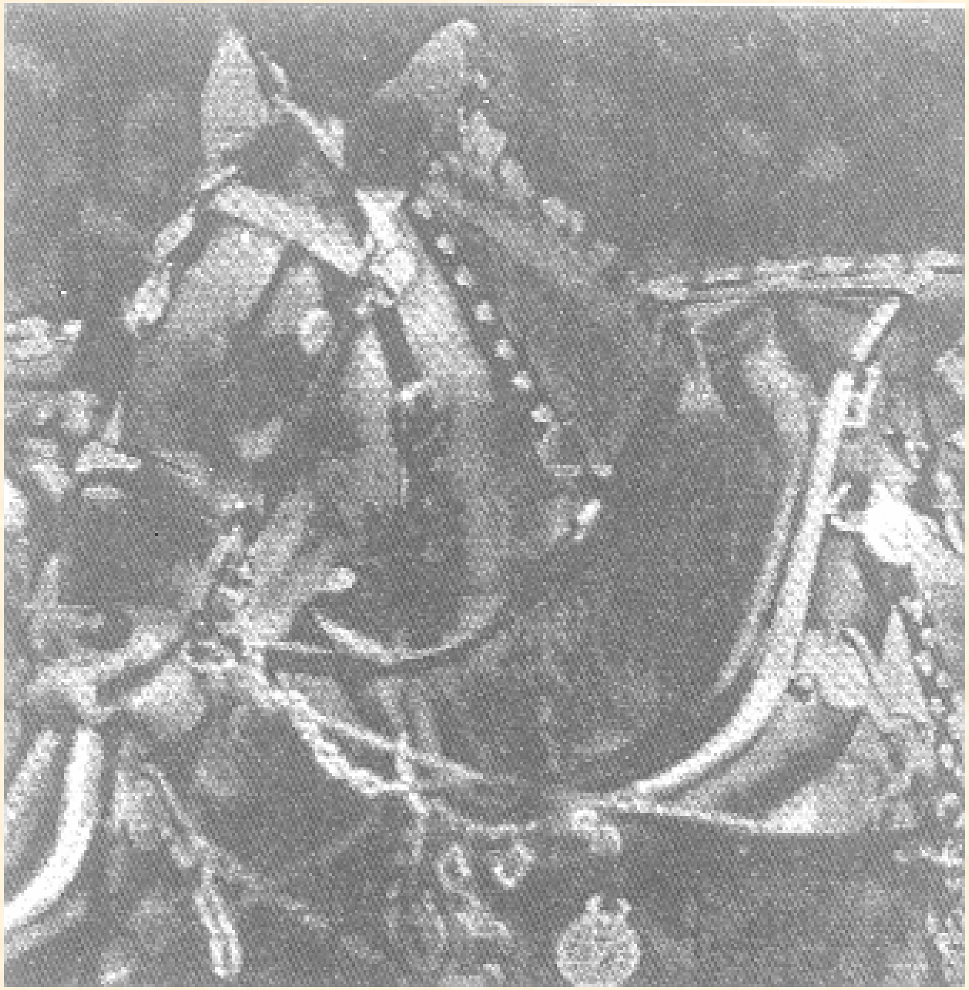
- Top Hat Transformation
  - The Morphological top-hat transformation is defined by

$$h = f - (f \circ b)$$

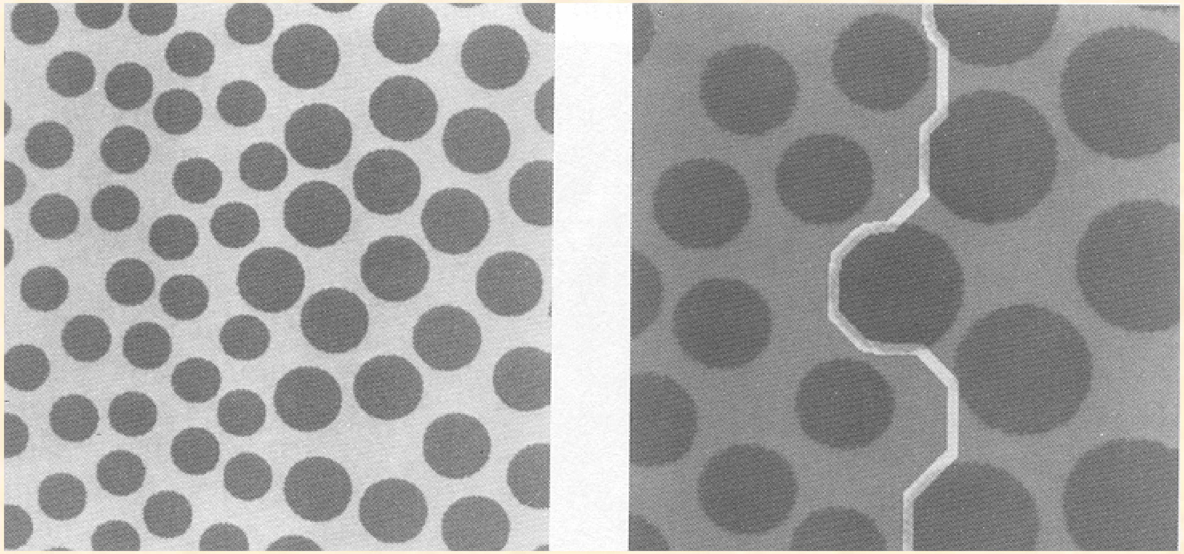
  - That is the image f minus its opening with a structuring element b, which is often of the form of a "top-hat." That is, a cylinder attached to a disk.
  - This transformation is useful for enhancing detail in the presence of shading
  - Also good in 1D for finding peaks that are, say, greater than a certain width and more than a certain depth (significant peaks)

Example

Top hat transformation of image
Note the enhanced detail



Texture Segmentation



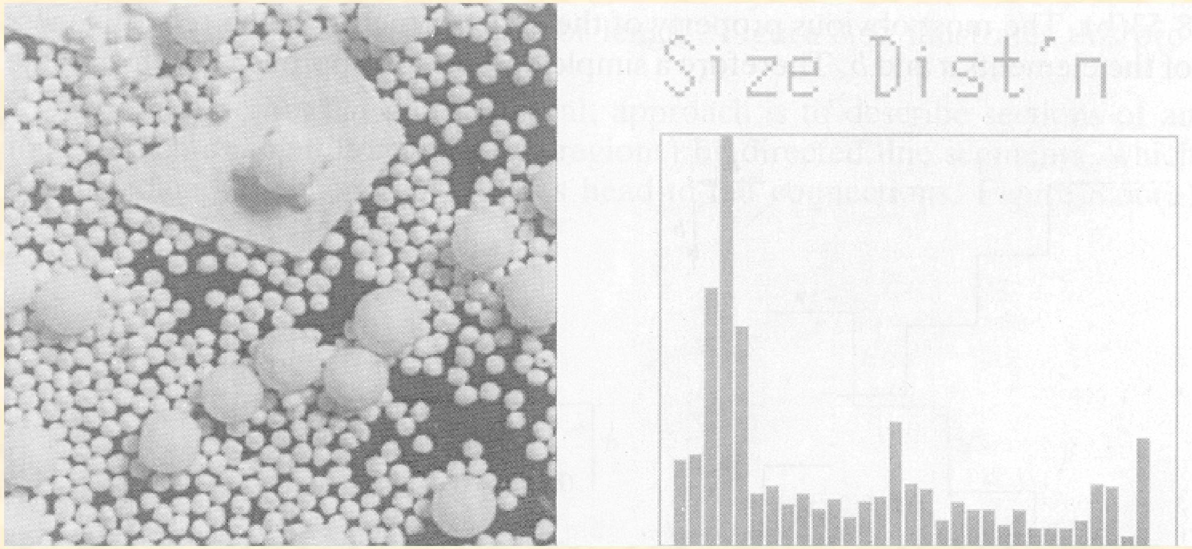
Method: Close with successively larger structuring elements until small dots disappear. Open remaining image with large structuring element and then threshold to determine textural boundary.

Consider interpretation with rolling ball – process resembles coin sorter

Granulometry

- Granulometry is a field that deals with the size distribution of particles
- In the example image (next slide), there are light objects of three different sizes
- The objects are overlapping and are too cluttered to detect individual objects

Example



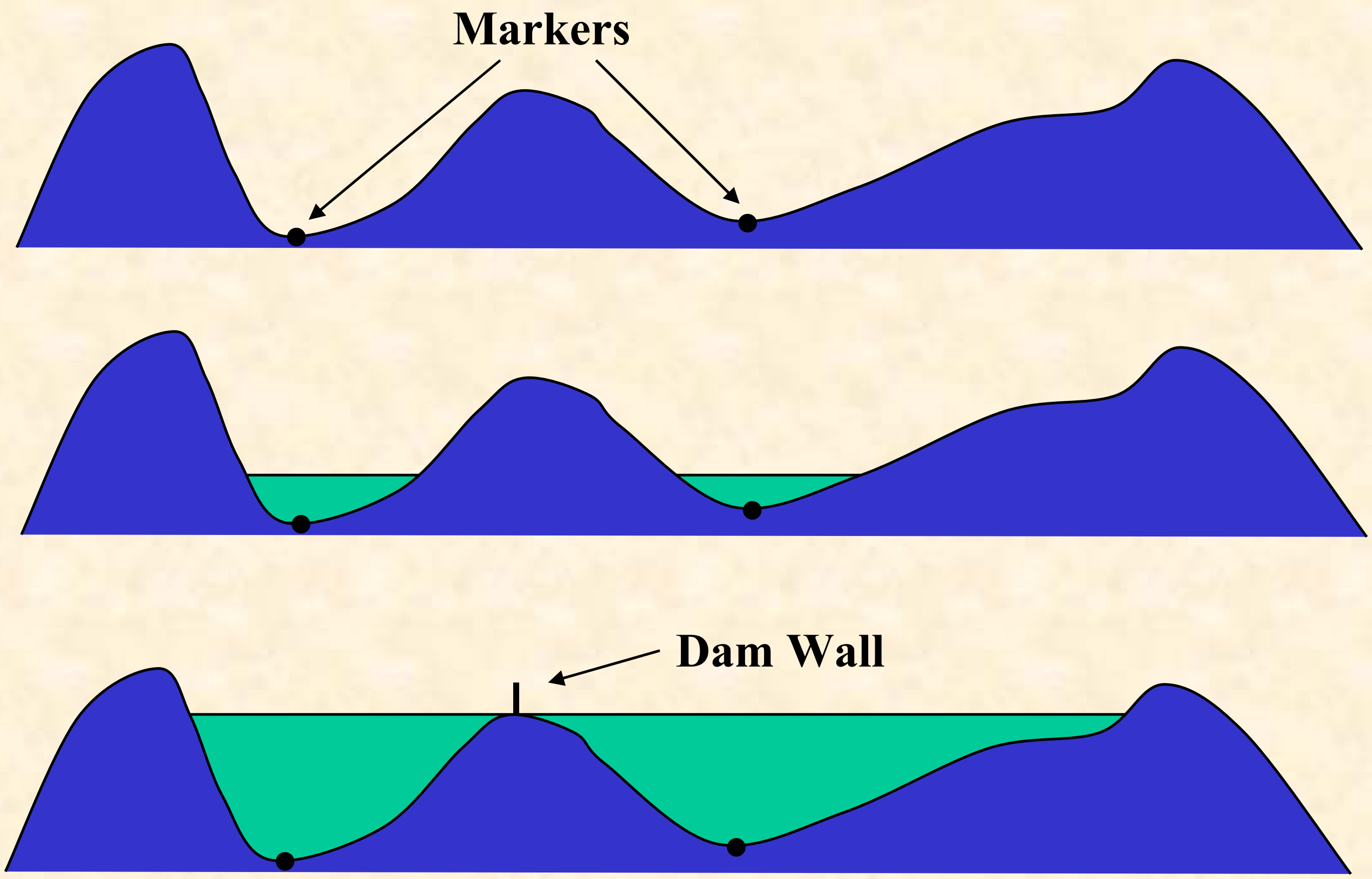
Method:

- opening operations with structuring elements of increasing size
- the difference between the original image and its opening is computed on each pass
- at the end of the process the differences are normalized and used to construct a histogram of particle size distribution

Watersheds

- Create markers on image (usually image gradient) to indicate regions of interest
- Visualize image as a topological surface (mountains and valleys)
- Flood object with a deluge of rain
- When waters from different regions meet, construct dams
- Once surface is completely flooded, the dam walls are our watershed segmentation.

Watershed Example



Problems with Watersheds

- Usually operates on the gradient image rather than the image itself
  - gradient accentuates noise
- Often difficult to determine appropriate markers in many applications
  - may lead to poor segmentation
- Found to be unsuitable for cell image segmentation application